## Prime Power Test (Hard)

Finite fields only exist when the order (size) is a prime power $p^{k}$ (where $p$ is a prime number and k is a positive integer). For each prime power, there is a finite field with this size, and all fields of a given order are isomorphic.
Finite fields are fundamental in a number of areas of mathematics and computer science, including number theory, algebraic geometry, Galois theory, finite geometry, cryptography and coding theory.

## Input

The first line contains an integer $T$, the number of test cases.
On the next $T$ lines, you will be given an integer $N$ : a proposed order to be tested.

## Output

Output $T$ lines, one for each test case, with $p k$ if $N$ can be the order of a finite field. $p$ must be a prime number, and $k$ an integer such that $N=p^{k}$. Else output "Invalid order".

## Example

## Input:

3
6
7
8

## Output:

Invalid order
71
23

## Constraints

$T$ about $2^{7}$, and $1<N<2^{33333}, N$ are $2^{128}$-smooth numbers. (Thanks at Min_25 for suggesting this constraint).
About $50 \%$ of input cases are "Invalid order". $N$ is log-uniform distributed between $2^{33333}$ and its square root.
Prime numbers in $N$ decomposition are almost log-uniform distributed, from 4bit to 128bit. 3 input files.
You may first try PRIMEPOW with easier constraints.

