## Periodic function, trip 1

xkcd/26
Let us consider periodic functions from $\mathbf{Z}$ to $\mathbf{R}$.
def $f(x)$ : return [4, -6, 7][x\%3] \# (with Python notations)
\# 4, -6, 7, 4, -6, 7, 4, -6, 7, 4, -6, 7, 4, -6, 7, ...
For example, $f$ is a 3-periodic function, with $f(0)=f(3)=f(6)=f(9)=4$.
With a simplified notation we will denote $f$ as $[4,-6,7]$.

For two periodic functions (with integral period), here the quotient of periods will be rational, in that case it can be shown that the sum of the functions is also a periodic function.
Thus, the set of all such functions is a vector space over $\mathbf{R}$.
Our interest, in this problem, will be the dimension of this space when the period is bounded by some integer $N$.

## Input

The first line contains an integer $T$, the number of test cases.
On the next $T$ lines, you will be given an integer $N$.
Consider the family of all $n$-periodic functions for $n$ in [1.. $N$ ]. There are some links between some functions.
For example: $[2,0]=[2,0,1,0]+[0,0,1,0]$, with simplified notations.

## Output

Print the rank of this family; ie the size of the largest collection of $\mathbf{R}$-linearly independent elements of this family.

## Example

## Input:

3
2
3
4
Output:
2
4
6

## Constraints

$0<T<10^{\wedge} 2$
$0<N<10^{\wedge} 8$
There's two input files, one easy (mostly small input), and a hard one (uniform random input).

My PY3.4 code get AC in 0.03+0.89=0.92s. This code isn't optimized.
I suspect there are several competitive approaches for this task.
Have fun ;-)

