GCD Determinant

English

<u>Vietnamese</u>

We say that a set $S = \{x1, x2, ..., xn\}$ is factor closed if for any $xi \in S$ and any divisor d of xi we have $d \in S$. Let's build a GCD matrix (S) = (sij), where sij = GCD(xi, xj) – the greatest common divisor of xi and xj. Given the factor closed set S, find the value of the determinant:

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D_n = \begin{vmatrix} \gcd(x_1, x_1) & \gcd(x_1, x_2) & \gcd(x_1, x_3) & \dots & \gcd(x_1, x_n) \\ \gcd(x_2, x_1) & \gcd(x_2, x_2) & \gcd(x_2, x_3) & \dots & \gcd(x_2, x_n) \\ \gcd(x_3, x_1) & \gcd(x_3, x_2) & \gcd(x_3, x_3) & \dots & \gcd(x_3, x_n) \\ \dots & \dots & \dots & \dots & \dots \\ \gcd(x_n, x_1) & \gcd(x_n, x_2) & \gcd(x_n, x_3) & \dots & \gcd(x_n, x_n) \end{vmatrix}
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Input

The input file contains several test cases. Each test case starts with an integer n (0 < n < 1000), that stands for the cardinality of S. The next line contains the numbers of S: x1, x2, ..., xn. It is known that each xi is an integer, $0 < xi < 2*10^9$. The input data set is correct and ends with an end of file.

Output

For each test case find and print the value Dn mod 100000007.

Sample