

# Fibonacci With a Square Root

FIBONACCI is the recursive sequence that is given by:  $F(n)=F(n-1)+F(n-2)$  with  $F(0)=0$  and  $F(1)=1$ .

In this problem we define FIBOSQRT that is given by:  $F_s(n)=F_s(n-1)+F_s(n-2)+2*\text{SQRT}(3+F_s(n-1)*F_s(n-2))$  with  $F_s(0)$  and  $F_s(1)$  are given in the input file.

It's guaranteed that  $\text{SQRT}(3+F_s(n-1)*F_s(n-2))$  is always an integer. 😊 I've proved it by math theorem.

Now your task is to find  $F_s(n)$ . Since the number can be big you have to find the result mod  $M$ .

## Input

The first line is an integer  $T(1 \leq T \leq 111,111)$ , denoting the number of test cases. Then,  $T$  test cases follow.

For each test case, there are four integers  $F_s(0)$ ,  $F_s(1)$  ( $1 \leq F_s(0) \leq F_s(1) < 10^6$ ),  $M$  ( $1 \leq M < 10^9$ ), and  $n$  ( $0 \leq n < 10^{18}$ ) written in one line, separated by space.

## Output

For each test case, output  $F_s(n) \bmod M$ .

## Example

**Input:**

```
2
1 1 10 5
2 3 100 6
```

**Output:**

```
4
82
```

## Explanation:

**Case #1:**

- $F_s(0)=1$
- $F_s(1)=1$
- $F_s(2)=1+1+2*\text{SQRT}(3+1*1)=6$
- $F_s(3)=6+1+2*\text{SQRT}(3+6*1)=13$
- $F_s(4)=13+6+2*\text{SQRT}(3+13*6)=37$
- $F_s(5)=37+13+2*\text{SQRT}(3+37*13)=94$

The answer is:  $94 \bmod 10 = 4$ .

**Case #2:**

- $F_s(0)=2$
- $F_s(1)=3$
- $F_s(2)=3+2+2*\text{SQRT}(3+3*2)=11$
- $F_s(3)=11+3+2*\text{SQRT}(3+11*3)=26$
- $F_s(4)=26+11+2*\text{SQRT}(3+26*11)=71$
- $F_s(5)=71+26+2*\text{SQRT}(3+71*26)=183$
- $F_s(6)=183+71+2*\text{SQRT}(3+183*71)=482$

The answer is:  $482 \bmod 100 = 82$ .

## Notes

File #1: More than 100,000 random test cases (test your program speed 😊)

File #2: Less than 10 test cases (tricky test cases that might give you WA 😊)

Time Limit  $\approx 8*(\text{My Program Top Speed})$

**Warning: large Input/Output data, be careful with certain languages**

**See also:** [Another problem added by Tjandra Satria Gunawan](#)