

# Divide Polygon (HARD)

This is hard version of [DTPOLY](#).

Determine the number of ways to cut a convex polygon with  $N$  vertices if the only cuts allowed are from vertex to vertex, each cut divides exactly one polygon into exactly two polygons, and you must end up with exactly  $K$  polygons. Consider each vertex distinct. For example, there are three ways to cut a square - the two diagonals and not cutting at all - but only two ways to cut it to form 2 polygons, and only one way to cut it to form 1 polygon. The order of cuts does not matter. Since the number of ways can be very large, you should return the number taken modulo  $M$ .

## Input

Input contains several test cases,  $i$ -th line consists of 3 integers:  $N_i$  ( $3 \leq N_i$ ,  $\sum N_i \leq 10^8$  over all test cases),

$K_i$  ( $1 \leq K_i \leq N_i - 2$ ) and  $M_i$  ( $1 < M_i < 2^{60}$ ), all pairs  $(N_i, K_i)$  are different.

## Output

On the  $i$ -th line print the number of different ways to cut the polygon with  $N_i$  vertices into  $K_i$  pieces modulo  $M_i$ .

## Example

### Input:

```
4 2 100
6 3 100
10000000 2 1000000007
10000000 5000000 1000000014000000049
```

### Output:

```
2
21
984650007
780127215155143528
```